

Задача 3.12.

ДАНЕ:

$$\lambda = 633 \text{ nm}$$

$$k = 200$$

$$r = 1 \text{ mm}$$

$$a = 1 \text{ m}$$

$$b = 0,5 \text{ m}$$

$$v = 2,25 \cdot 10^8 \frac{\text{m}}{\text{s}}$$

$$c = 3 \cdot 10^8 \frac{\text{m}}{\text{s}}$$

A) $d = \frac{r}{k}$

$$d = \frac{10^{-3}}{200} = 5 \cdot 10^{-6} \text{ m} = \underline{5 \mu\text{m}}$$

B)

$$n \cdot \lambda = d \cdot \sin \alpha$$

$$d \cdot \sin \alpha = 1 \cdot \lambda$$

$$\sin \alpha = \frac{\lambda}{d}$$

$$\text{tg } \alpha = \frac{\Delta y}{b} \rightarrow \Delta y = b \cdot \text{tg } \alpha$$

$$\text{tg } \alpha = \frac{\sin \alpha}{\cos \alpha}$$

$$\Delta y = b \cdot \frac{\sin \alpha}{\sqrt{1 - \sin^2 \alpha}} \rightarrow \text{вспомогательная}$$

$$\Delta y = b \cdot \frac{\frac{\lambda}{d}}{\sqrt{1 - \left(\frac{\lambda}{d}\right)^2}} = b \cdot \frac{\frac{\lambda}{d}}{\sqrt{1 - \frac{\lambda^2}{d^2}}} = b \cdot \frac{\frac{\lambda}{d}}{\sqrt{\frac{d^2 - \lambda^2}{d^2}}} =$$

$$b \cdot \frac{\frac{\lambda}{d}}{\frac{1}{d} \cdot \sqrt{d^2 - \lambda^2}} = \underline{\underline{b \cdot \frac{\lambda}{\sqrt{d^2 - \lambda^2}}}}$$

$$\Delta y = 0,5 \text{ m} \cdot \frac{633 \cdot 10^{-9} \text{ m}}{\sqrt{(5 \cdot 10^{-6} \text{ m})^2 - (633 \cdot 10^{-9} \text{ m})^2}} = \frac{316,5 \cdot 10^{-9}}{\sqrt{24,599311 \cdot 10^{-12}}} \approx$$

$$\frac{316,5 \cdot 10^{-9} \text{ m}}{4,96 \cdot 10^{-6} \text{ m}} \approx 63,81 \cdot 10^{-3} \text{ m} = 6,381 \text{ cm} \approx \underline{6,4 \text{ cm}}$$

c) $y = \frac{a}{2}$
 $\text{tg } \alpha = \frac{y}{b} \rightarrow \frac{\frac{a}{2}}{b} \rightarrow \frac{a}{2b}$

$$\underline{\underline{m = 2 \cdot n + 1 = 11}}$$

$$\text{tg } \alpha = \frac{1}{2 \cdot 0,5} = \underline{1}$$

$$\alpha = 45^\circ$$

$$n \cdot \lambda = d \cdot \sin \alpha$$

$$n = \frac{a}{\lambda} \cdot \sin \alpha \rightarrow \frac{5 \cdot 10^{-6}}{633 \cdot 10^{-9}} \cdot \sin 45^\circ \approx$$

$$0,0079 \cdot 10^3 \cdot 0,7071 \approx 5,58609 \Rightarrow \underline{\underline{n = 5}}$$

$$d) \lambda = \frac{v}{f} \Rightarrow f = \frac{v}{\lambda}$$

$$f_p = \frac{c}{\lambda} \quad f_w = \frac{v}{\lambda_w}$$

$$f_p = f_w$$

$$\frac{c}{\lambda} = \frac{v}{\lambda_w}$$

$$c \cdot \lambda_w = v \cdot \lambda$$

$$\lambda_w = \lambda \frac{v}{c}$$

$$\lambda = \frac{d \cdot \sin \alpha}{n}$$

$$E) \lambda_w = \lambda \cdot \frac{v}{c}$$

$$\lambda_w = 633 \cdot 10^{-9} \text{ m} \cdot \frac{2,25 \cdot 10^8 \text{ m/s}}{3 \cdot 10^8 \text{ m/s}} = 474,75 \cdot 10^{-9} \text{ m}$$

$$\Delta y = b \cdot \frac{\lambda_w}{\sqrt{a^2 - \lambda_w^2}}$$

$$\Delta = 0,5 \text{ m} \cdot \frac{474,75 \cdot 10^{-9} \text{ m}}{\sqrt{(5 \cdot 10^{-4} \text{ m})^2 - (474,75 \cdot 10^{-9} \text{ m})^2}} = \frac{237,375 \cdot 10^{-9} \text{ m}^2}{\sqrt{241775 \cdot 10^{-12} \text{ m}^2}} \approx$$

$$475,69 \cdot 10^{-9} \text{ m} \approx \underline{\underline{4,8 \mu\text{m}}}$$

$$F) \sin \alpha = 45^\circ$$

$$n = \frac{d}{\lambda_w} \cdot \sin \alpha$$

$$n = \frac{5 \cdot 10^{-6}}{474,75 \cdot 10^{-9} \text{ m}} \cdot \sin 45^\circ = 7,071$$

$$\underline{\underline{n = 7}}$$